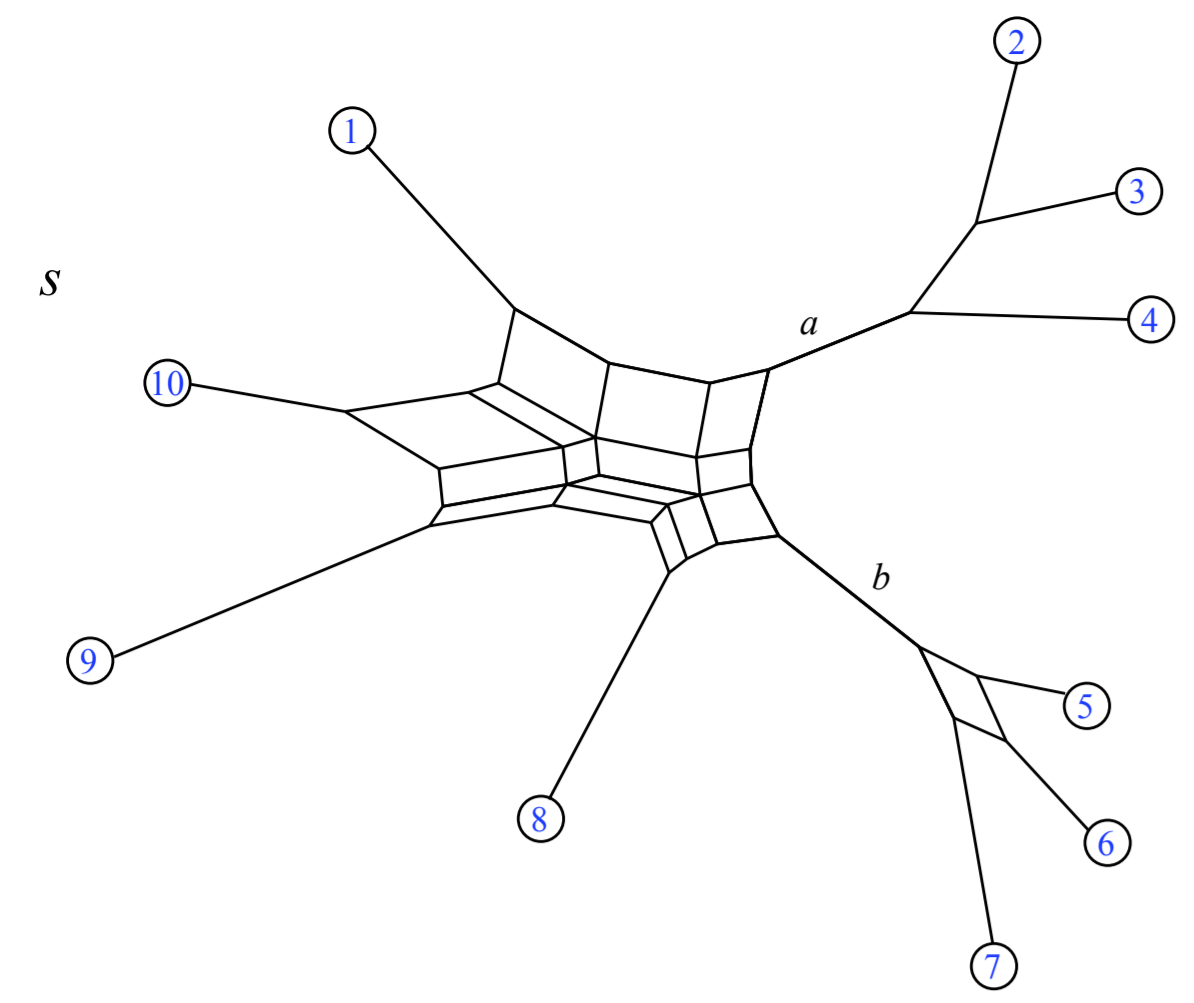


Starting with *M* (experimental) we use the formula to get *W*, and then use Neighbor-net to find the splits.

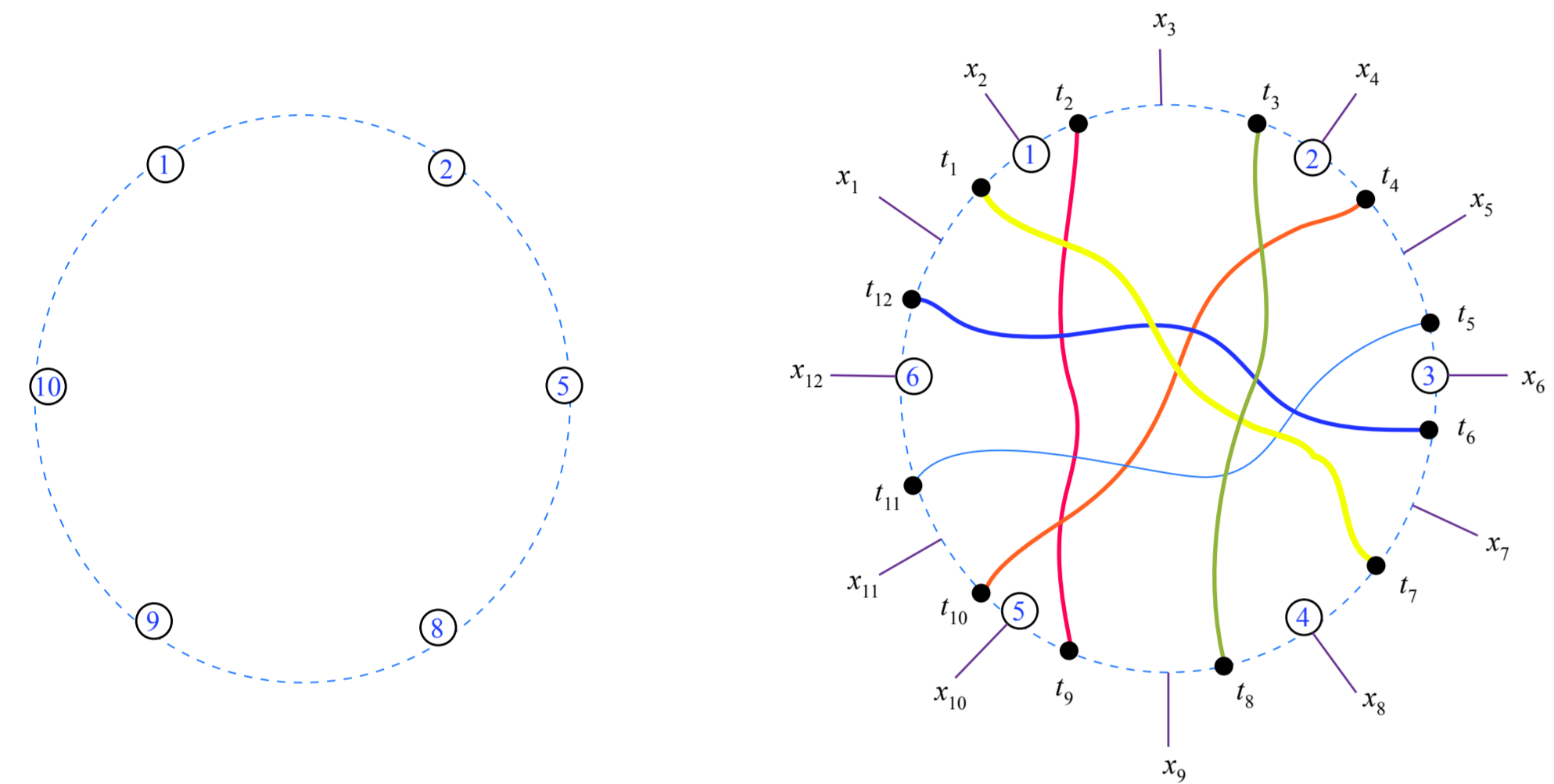
M = matrix with 10 columns and 10 rows of numerical values.



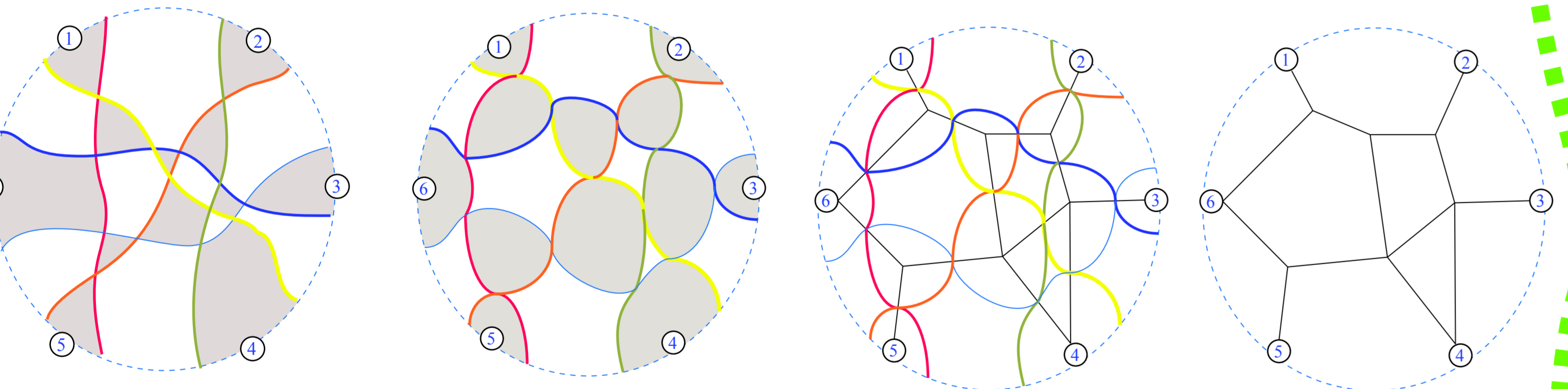
NumTerminals (6) = matrix, MaxRespected (S) = matrix, Re-entrants (S) = matrix.

That allows us to isolate the blobs. First we check the bridges a and b to see if they are real network features. For potential bridge b the connections that suffice are those connections involving path 5--7, but involving at most one node from {2,3,4}, since that cluster is also separated by a split.

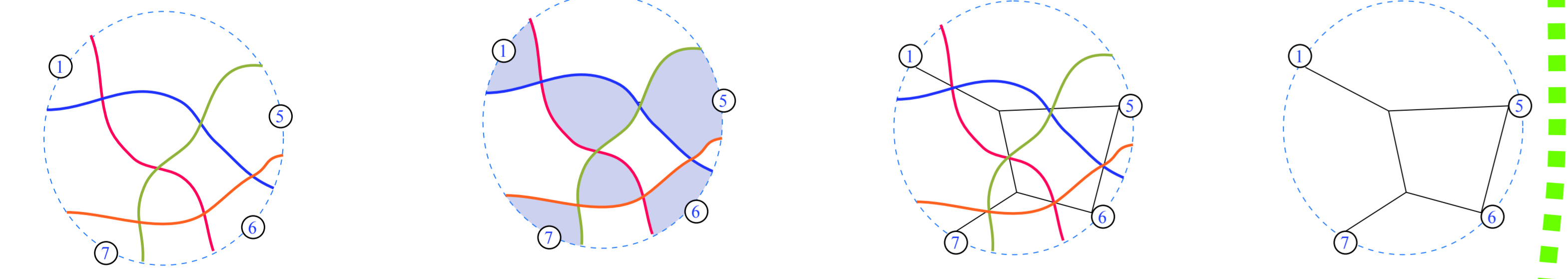
Now we find the blob of size 6. We choose a terminal connected by an internal path to each of its corners: here we chose {1,2,5,8,9,10}. We label those as 1-6. We let P = W|_{1,2,5,8,9,10}, restricted to those terminals. Then S is the response matrix associated to P, and we use S to find the matrix MR = MaxRespected(S), where entry MR(i,j) is the size of the largest k-connection that respects the cut from x_i to x_j.



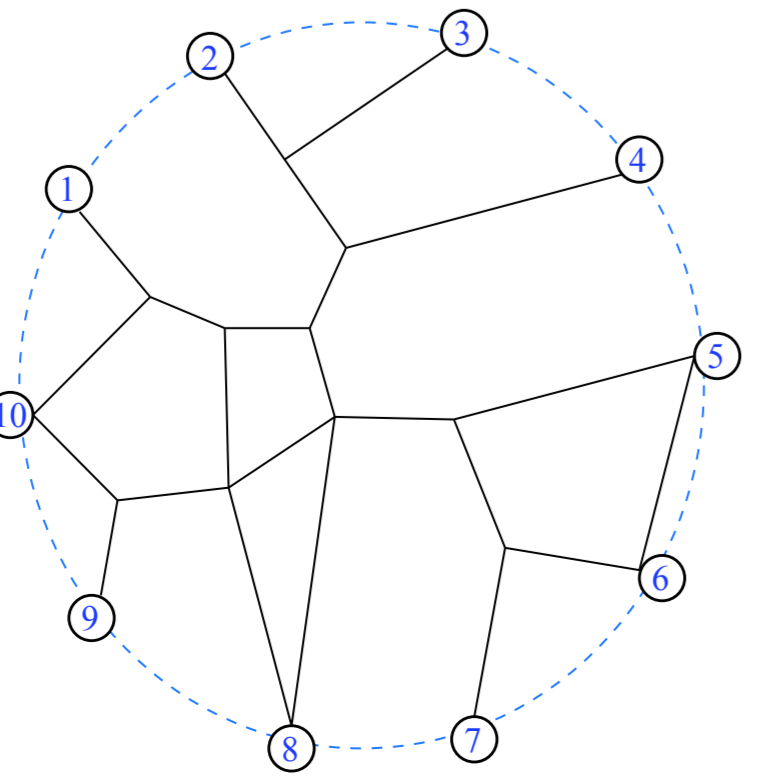
Next we draw the local network for the blob by placing a node in each shaded region (strating with the terminals).



The process is repeated for the size 4 blob, using the matrix Q which is W restricted to terminals {1,5,6,7}, and T which is the response matrix associated to Q.



Finally the blobs and treelike portion are rejoined to see the full network.



Matlab

```
>> A=[1 0 0 0 0 0 0 0 0 0; 0 -2 0 0 0 0 0 0 0 0; 0 0 -1 0 0 0 0 0 0 0; 0 0 0 -5 0 0 0 0 0 0; 0 0 0 0 -6 2 0 0 0 0; 0 0 0 0 2 -5 0 0 0 0; 0 0 0 0 0 0 -1 0 0 0; 0 0 0 0 0 0 0 -3 0 0; 0 0 0 0 0 0 0 0 -1 0; 0 0 0 0 0 0 0 0 0 -3]
>> B=[1 0 0 0 0 0 0 0 0 0; 0 0 0 1 0 0 0 0 0 0; 0 0 0 0 1 0 0 0 0 0; 0 0 0 0 0 1 0 0 0 0; 0 0 0 0 0 0 1 0 0 0; 0 0 0 0 0 0 0 1 0 0; 0 0 0 0 0 0 0 0 1 0; 0 0 0 0 0 0 0 0 0 1; 0 0 0 0 0 0 0 0 0 0; 0 0 0 0 0 0 0 0 0 0]
>> C=[-4 2 0 0 0 0 0 0 0 0; 2 -6 3 0 0 0 0 0 0 0; 0 3 -7 2 0 0 0 0 0 0; 0 0 2 -10 3 0 0 0 0 0; 0 0 0 3 -6 0 0 0 0 0; 0 0 0 0 0 -12 5 3 0 0; 0 0 0 0 0 5 -9 0 0 0; 0 0 2 0 0 3 0 -8 2 0; 0 1 0 0 0 0 0 2 -6 3; 0 1 0 0 0 0 0 0 2 -6 3]
>> M=A-B*(C^(-1))*B
>> pinv(M)
>> Z=diag(Z)
>> D=diag(Z)
>> J=[1 1 1 1 1 1 1 1 1 1; 1 1 1 1 1 1 1 1 1 1; 1 1 1 1 1 1 1 1 1 1; 1 1 1 1 1 1 1 1 1 1; 1 1 1 1 1 1 1 1 1 1; 1 1 1 1 1 1 1 1 1 1; 1 1 1 1 1 1 1 1 1 1; 1 1 1 1 1 1 1 1 1 1; 1 1 1 1 1 1 1 1 1 1; 1 1 1 1 1 1 1 1 1 1]
>> D=diag(diag(Z))
>> T=[-0.4453 0.2863 0.1193 0.0398; 0.2863 -3.6126 2.9948 0.3316; 0.1193 2.9948 -3.5855 0.4715; 0.0398 0.3316 0.4715 -0.8428]
>> 0.039758785128941*2.994750914394186 - 0.119276355386824*0.331583638131394
ans =
0.0795
>> 0.286263252928376*0.471493182554749 - 0.119276355386824*0.331583638131394
ans =
0.0954
```

SplitsTree interface showing #NEXUS, BEGIN tax, and BEGIN distances; DIMENSIONS ntax=10; TAXLABELS [1] one [2] two [3] three [4] four [5] five [6] six [7] seven [8] eight [9] nine [10] ten; and FORMAT triangle=LOWER labels.

```
W =
0 2.9693 3.4693 2.3359 2.2863 2.3967 3.2538 1.9612 2.7189 1.6528
2.9693 0 1.5000 1.0333 2.2370 2.3474 3.2045 2.0386 3.0102 2.1701
3.4693 1.5000 0 1.5333 2.7370 2.8474 3.7045 2.5386 3.5102 2.6701
2.3359 1.0333 1.5333 0 1.6036 1.7140 2.5712 1.4052 2.3769 1.5368
2.2863 2.2370 2.7370 1.6036 0 0.3052 1.2922 1.0019 2.0914 1.3299
2.3967 2.3474 2.8474 1.7140 0.3052 0 1.2468 1.1123 2.2018 1.4403
3.2538 3.2045 3.7045 2.5712 1.2922 1.2468 0 1.9694 3.0589 2.2975
1.9612 2.0386 2.5386 1.4052 1.0019 1.1123 1.9694 0 1.6485 0.9263
2.7189 3.0102 3.5102 2.3769 2.0914 2.2018 3.0589 1.6485 0 1.4132
1.6528 2.1701 2.6701 1.5368 1.3299 1.4403 2.2975 0.9263 1.4132 0

>> format long
>> W
W =
Columns 1 through 7
0 2.969250363901018 3.469250363901019 2.335917030567686 2.286269589217186 2.396659199606797 3.253802056749655
2.969250363901016 0 1.500000000000002 1.033333333333333 2.236961001153138 2.347350611542748 3.204493468685606
3.469250363901017 1.499999999999998 0 1.533333333333334 2.736961001153140 2.847350611542750 3.704493468685607
2.335917030567684 1.033333333333333 1.533333333333334 0 1.603627667819806 1.714017278209417 2.571160135352274
2.286269589217186 2.236961001153141 2.736961001153142 1.603627667819807 0 0.305194805194805 1.292207792207792
2.396659199606797 2.347350611542751 2.847350611542751 1.714017278209417 0.305194805194805 0 1.246753246753247
3.253802056749654 3.204493468685608 3.704493468685608 2.571160135352274 1.292207792207792 1.246753246753246 0
1.961245441484715 2.038573508005823 2.538573508005823 1.405240174672489 1.001880942928977 1.11227055318588 1.969413410461446
2.71888462882094 3.010189228529838 3.510189228529838 2.376855895196506 2.091400593583998 2.201790203973609 3.05893061116466
1.652838427947597 2.170123726346434 2.670123726346434 1.53679039013101 1.329937711487929 1.440327321877540 2.297470179020397

Columns 8 through 10
1.961244541484716 2.71888462882095 1.652838427947598
2.038573508005822 2.010189228529838 1.652838427947598
2.538573508005822 3.510189228529840 2.670123726346432
1.405240174672488 2.376855895196507 1.53679039013099
1.001880942928977 2.091400593583999 1.329937711487929
1.112270553185887 2.201790203973609 1.440327321877539
1.969413410461444 3.05893061116466 2.297470179020396
0 1.648471615720524 0.926310043668122
1.648471615720523 0 1.413209606986899
0.926310043668121 1.413209606986899 0

>> format short
P =
0 2.9693 2.2863 1.9612 2.7189 1.6528
2.9693 0 2.2370 2.0386 3.0102 2.1701
2.2863 2.2370 0 1.0019 2.0914 1.3299
1.9612 2.0386 1.0019 0 1.6485 0.9263
2.7189 3.0102 2.0914 1.6485 0 1.4132
1.6528 2.1701 1.3299 0.9263 1.4132 0

>> J=[1 1 1 1 1 1; 1 1 1 1 1 1; 1 1 1 1 1 1; 1 1 1 1 1 1; 1 1 1 1 1 1]
J =
1 1 1 1 1 1
1 1 1 1 1 1
1 1 1 1 1 1
1 1 1 1 1 1
1 1 1 1 1 1

>> S=pinv(S*(P-(1/6)*(P*J+J*P)+(trace(P*J)/36)*J))
S =
-0.6653 0.0770 0.0770 0.1186 0.0194 0.3734
0.0770 -0.5699 0.1578 0.1836 0.0248 0.1267
0.0770 0.1578 -1.1711 0.6513 0.0694 0.2157
0.1186 0.1836 0.6513 -1.7491 0.2257 0.5699
0.0194 0.0248 0.0694 0.2257 -0.7862 0.4470
0.3734 0.1267 0.2157 0.5699 0.4470 -1.7326

>> format long
>> S
S =
-0.665327287290690 0.077002490404231 0.077002490404231 0.118592406040652 0.019358582738092 0.373389878185495
0.077002490404231 -0.569905786993309 0.157778945484152 0.183649782677378 0.024824026007772 0.126650542419775
0.077002490404231 0.157778945484152 -1.171146617084058 0.651314535827093 0.069361758642792 0.215707447207803
0.118592406040654 0.183649782677379 0.651314535827093 -1.749136525131306 0.225662464848509 0.569917335737672
0.019358582738092 0.024824026007772 0.069361758642792 0.225662464848509 -0.786188471658419 0.446981639421254
0.373389878185494 0.126650542419775 0.215707447207802 0.569917335737673 0.446981639421254 -1.732646842971999

Q =
0 2.286269589217186 2.396659199606797 3.253802056749655
2.286269589217186 0 0.305194805194805 1.292207792207792
2.396659199606797 0.305194805194805 0 1.246753246753247
3.253802056749654 1.292207792207792 1.246753246753246 0

J =
1 1 1 1
1 1 1 1
1 1 1 1
1 1 1 1

>> T=pinv(L*(Q-(1/4)*(Q*J+J*Q)+(trace(Q*J)/16)*J))
T =
-0.445298393444141 0.286263252928376 0.119276355386824 0.039758785128941
0.286263252928376 -3.612597805453960 2.994750914394186 0.331583638131394
0.119276355386824 2.994750914394186 -3.58520452335756 0.471493182554749
0.039758785128941 0.331583638131392 0.471493182554751 -0.842835605815084
```

```
T =
-0.4453 0.2863 0.1193 0.0398
0.2863 -3.6126 2.9948 0.3316
0.1193 2.9948 -3.5855 0.4715
0.0398 0.3316 0.4715 -0.8428

>> 0.039758785128941*2.994750914394186 - 0.119276355386824*0.331583638131394
ans =
0.0795

>> 0.286263252928376*0.471493182554749 - 0.119276355386824*0.331583638131394
ans =
0.0954
```