Linear. Quiz 5. Name \_\_\_\_\_ Consider the following sets of polynomials in  $\mathcal{P}_2$ .

$$\mathcal{A} = \{x - 1, x, x^2 + 1\}, \ \mathcal{B} = \{3x^2, x, x + 2, 3\}, \ \mathcal{C} = \{3x^2, x^2 - 1, x + 2\},$$
$$\mathcal{D} = \{3x^2, x + 2\}, \ \mathcal{F} = \{x^2, x + 2, 3x^2 + 3x + 6\}$$

(1) Which two are lin. dep.?

(2) Which two do not span  $\mathcal{P}_2$ ?

(3) Which two are bases for  $\mathcal{P}_2$ ?

(4) For both bases you just found, in alphabetic order, find the coordinate vector for  $5x^2 + 7x$ . (Two answers.)

(5) These five lines are described by a matrix equation  $A\mathbf{x} = \mathbf{b}$ . Does  $\mathbf{b} = \mathbf{0}$ ?\_\_\_\_\_ Does a solution  $\mathbf{x}$  exist?\_\_\_\_\_ Are the columns of A lin. indep. or lin. dep.?\_\_\_\_\_ Are the rows of A a basis?\_\_\_\_\_