

$P \wedge Q$


GATE: 

TABLE:

P	Q	$P \wedge Q$
T	T	T
T	F	F
F	T	F
F	F	F

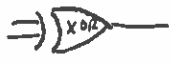
NEGATION SIMPLIFIED: $\sim(P \wedge Q) = \sim P \vee \sim Q$

$P \vee Q$


GATE: 

NEGATION SIMPLIFIED: $\sim(P \vee Q) = \sim P \wedge \sim Q$

$P \text{ XOR } Q$

GATE: 

$\sim P$

GATE: 

HA (Half Adder):

P, Q inputs → HA box → carry (2's place), sum (1's place) outputs

FA (Full Adder):

P, Q, R inputs → FA box → carry (2's place), sum (1's place) outputs

$P \Rightarrow Q$

TABLE:

P	Q	$P \Rightarrow Q$
T	T	T
T	F	F
F	T	T
F	F	T

True \Rightarrow False is F

NEGATION SIMPLIFIED: $\sim(P \Rightarrow Q) = P \wedge \sim Q$

original implication $P \Rightarrow Q$

P implies Q
 if P then Q
 Q , if P
 P only if Q
 P is sufficient for Q
 Q is necessary for P

biconditional $P \Leftrightarrow Q$

$= P \Rightarrow Q \wedge Q \Rightarrow P$

$= P$ if and only if Q

$= P$ necessary and sufficient for Q

converse $Q \Rightarrow P$

contrapositive $\sim Q \Rightarrow \sim P$

inverse $\sim P \Rightarrow \sim Q$

negation $P \wedge \sim Q$

- tautology: all T
- contradiction: all F
- valid / in valid } when premises T then conclusion T

$\forall P, Q.$ = for all $P, Q.$ } $\sim(\forall P, Q) = \exists P \text{ s.t. } \sim Q.$

$\exists P \text{ s.t. } Q.$ = there exists $P \text{ s.t. } Q.$ } $\sim(\exists P \text{ s.t. } Q) = \forall P, \sim Q.$

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