

Combinatorics. Quiz 6b. Name _____ Time _____

Show all work for full or partial credit. Put a box around your final answer in each part. Try the problem on your own before helping each other understand it.

1. Find the exponential generating function for the sequence h_n where h_n is the number of permutations of length n using the letters A, C, G, T , with repetition.

2. a) Find the e.g.f. for the sequence b_n where b_n is the number of permutations of length n using the letters A, C, G, T , but there is at least 1 G and an even number of T 's.
b) Use the answer above to find a closed formula for b_n .
c) Check that the formula gives the right answer for $n = 3$ (list by hand all the 3-perms that obey the requirements.)
d) Check that the third derivative of the e.g.f at zero also gives that answer. (wolframalpha.com, turn in screen shot.)