

Ex: Find a normal vector of the plane or the direction vector of the line.

- 1) Plane including point $P = (1, 2, -3)$ and including line $L = \begin{cases} x = 1 \\ y = -2t \\ z = 1+t \end{cases}$.

Find \vec{n}

L has direction $\vec{u} = \langle 0, -2, 1 \rangle$ and point $(1, 0, 1)$

$$\vec{n} = \langle 0, -2, 1 \rangle \times \vec{QP} \quad \text{where } Q = (1, 0, 1)$$

$$= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 0 & -2 & 1 \\ 0 & 2 & -4 \end{vmatrix} = \langle 6, 0, 0 \rangle.$$

- 2) Plane \perp to line $\frac{x}{3} = y+1 = \frac{z+2}{-1}$.

$$\vec{n} = \vec{u} \text{ of line! line: } t = \frac{x}{3}, t = y+1, t = \frac{z+2}{-1}$$

$$\vec{n} = \langle 3, -1, -1 \rangle$$

$$\Rightarrow \begin{cases} x = 3t \\ y = -1+t \\ z = -t-2 \end{cases}$$

- 3) Line \perp to plane $3x - y + \frac{1}{2}z = 2$

$$\text{Find } \vec{u} = \vec{n} = \langle 3, -1, \frac{1}{2} \rangle$$