



$\int_C \vec{F} \cdot d\vec{r}$	$\nabla \times \vec{F} \neq \vec{0}$	$\nabla \times \vec{F} = \vec{0}$
any C	$\int P dx + Q dy + R dz$ and substitute $t$	$[f_p]$ finish start by FTVC
C closed	C simple, on surface $\iint_D (\nabla \times \vec{F}) \cdot (-\vec{n}) dA$ Stokes / Greens	$0$ by FTVC

$(-\vec{n} = \langle -f_x, -f_y, 1 \rangle)$  ( $f_p = \text{potential}$ )

### Scalars

$$V = \iint_D f(x, y) dA \quad ; \quad \text{type I} \Rightarrow dy dx \quad \text{type II} \Rightarrow dx dy$$

polar  $\Rightarrow r dr d\theta$

$$\text{mass} = \iiint_D f(x, y, z) dV \quad ; \quad \text{type I} \Rightarrow dz dy dx$$

type II  $\Rightarrow dz dx dy$

$$V = \iiint_D 1 dV \quad ;$$

cylindrical  $\Rightarrow r dz dr d\theta$   
spherical  $\Rightarrow \rho^2 \sin \phi d\rho d\theta d\phi$

$$\text{div}(\vec{F}) = \nabla \cdot \vec{F} = \partial_x P + \partial_y Q + \partial_z R = P_x + Q_y + R_z$$

### Vectors

$$\text{curl}(\vec{F}) = \nabla \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \partial_x & \partial_y & \partial_z \\ P & Q & R \end{vmatrix} = \langle R_y - Q_z, -(R_x - P_z), Q_x - P_y \rangle$$

If  $\nabla \times \vec{F} = \vec{0}$ , (smooth + continuous  $\vec{F}$ ),  $\vec{F}$  is conservative, gradient, path indep.

then we can find potential  $f(x, y, z)$  with  $\vec{F} = \nabla f$ .

$$\text{flux} = \iint_S \vec{F} \cdot d\vec{s} = \iint_D \vec{F} \cdot (-\vec{n}) dA$$

Unbounded surface of 3D volume  $E$  } flux =  $\iiint_E \nabla \cdot \vec{F} dV$