

Calculus II. Review for Test 2.

1. Find these definite integrals and classify as “divergent” or “convergent”:

a) $\int_3^{\infty} xe^{-x^2} dx$

b) $\int_{-1}^0 \frac{3}{x^5} dx$

c) $\int_{-2}^{14} \frac{1}{\sqrt[4]{x+2}} dx$

2. For each of these sequences, find the limits, if they exist, and decide “diverges” or “converges.”

a) $\lim_{n \rightarrow \infty} \frac{2^n + n}{3^n + 1}$

b) $\lim_{n \rightarrow \infty} \frac{n + 4n^3}{2n^4 + 1}$

c) $\lim_{n \rightarrow \infty} \frac{n^3 + n^2}{7n^3 + 1}$

d) $\lim_{n \rightarrow \infty} \frac{7}{\cos(n\pi)}$

e) $\lim_{n \rightarrow \infty} \frac{\tan^{-1}(n)}{3}$

f) $\lim_{n \rightarrow \infty} \frac{(-1)^n}{3^n}$

g) $\lim_{n \rightarrow \infty} \frac{3^n(-1)^n}{2^n}$

3. For each series, what does the limit test for divergence tell us? [converge, diverge, or inconclusive] Show your work by performing the test.

$$a) \sum_{n=1}^{\infty} \frac{e^{2n} + 3n}{5e^{2n} - 6}$$

$$b) \sum_{n=1}^{\infty} \frac{2^n}{3^n}$$

$$c) \sum_{n=1}^{\infty} \frac{3}{e^{2n}}$$

4. For each series, what does the geometric series test tell us? [not applicable, converge, diverge, or inconclusive] Show your work, and find the value if it converges.

$$a) \sum_{n=1}^{\infty} \frac{3^n}{\pi^n}$$

$$b) \sum_{n=1}^{\infty} \frac{5^n}{(\sqrt{3})^n}$$

$$c) \sum_{n=1}^{\infty} \frac{3}{(0.5)^n}$$

$$d) \sum_{n=1}^{\infty} \frac{1}{(-2)^n}$$

$$e) \sum_{n=1}^{\infty} \frac{3}{e^{2n}}$$

$$f) \sum_{n=1}^{\infty} \frac{n}{e^{2n}}$$

5. For each series, what does the p -series test tell us? [not applicable, converge, diverge, or inconclusive] Show your work.

$$a) \sum_{n=1}^{\infty} \frac{5^n}{(\sqrt{3})^n}$$

$$b) \sum_{n=1}^{\infty} \frac{3}{n^{(0.5)}}$$

$$c) \sum_{n=1}^{\infty} \frac{2}{n}$$

$$d) \sum_{n=1}^{\infty} \left(\frac{1}{n}\right)^3$$

6. For each series, what does the integral test tell us? [not applicable, converge, diverge, or inconclusive] Show your work.

$$a) \sum_{n=1}^{\infty} \frac{\sqrt{n} + 4}{n^2}$$

$$b) \sum_{n=1}^{\infty} \frac{1}{\sqrt{n} + 1}$$

$$c) \sum_{n=1}^{\infty} \left(\frac{1}{n}\right)^3$$

$$d) \sum_{n=1}^{\infty} \frac{1}{(-2)^n}$$

$$e) \sum_{n=1}^{\infty} \frac{1}{\cos^2(n)}$$

7. For each series, what does the comparison test tell us? [not applicable, converge, or diverge] Show your work.

$$a) \sum_{n=1}^{\infty} \frac{1}{2n^3 + 1}$$

$$b) \sum_{n=1}^{\infty} \frac{9^n}{3 + 10^n}$$

$$c) \sum_{n=1}^{\infty} \frac{6^n}{-4 + 5^n}$$

$$d) \sum_{n=1}^{\infty} \frac{(-1)^n}{-4 + 5^n}$$

8. For each series, what does the limit comparison test tell us? [not applicable, converge, or diverge] Show your work.

$$a) \sum_{n=1}^{\infty} \frac{1}{2n + 1}$$

$$b) \sum_{n=1}^{\infty} \frac{n + 2}{(n + 1)^3}$$

$$c) \sum_{n=1}^{\infty} \frac{2^n}{5^n - n}$$

9. For each series, use the alternating series test or the limit test for divergence to decide: [converge, or diverge]. Show your work.

$$a) \sum_{n=1}^{\infty} \frac{(-1)^n}{\ln(n+1)}$$

$$b) \sum_{n=1}^{\infty} \frac{(-1)^n}{4n+1}$$

$$c) \sum_{n=1}^{\infty} \frac{(-1)^n}{e^{-n}}$$

10. Decide if the sums converge or diverge, explain why. If there is a formula for the sum, find the value.

$$a) \sum_{n=1}^{\infty} n^2 e^{-n^3}$$

$$b) \sum_{n=1}^{\infty} e^{2n}$$

$$c) \sum_{n=1}^{\infty} \frac{2^n}{e^{3n}}$$

11. For each series, what does the ratio test tell us? [converge absolutely, diverge, or inconclusive]. Show your work by finding the limit.

$$(a) \sum_{n=1}^{\infty} \frac{(-2)^n}{n!}$$

$$(b) \sum_{n=1}^{\infty} \frac{2^{(n^2)}}{(2n)!}$$

12. For each series, what does the root test tell us? [converge absolutely, diverge, or inconclusive]. Show your work by finding the limit.

$$(a) \sum_{n=1}^{\infty} \left(\frac{-2n}{3n+1} \right)^n$$

$$(b) \sum_{n=1}^{\infty} \left(\frac{1}{\sqrt{n}} \right)^n$$

13. For this power series, determine the radius of convergence.

$$\sum_{n=1}^{\infty} \frac{2(x-3)^n}{n5^n}$$

14. For this power series, the radius of convergence is found to be $R = 3$. Determine the interval of convergence.

$$\sum_{n=1}^{\infty} \frac{(x-2)^n}{n3^{(n+1)}}$$

15. For this power series, determine the interval of convergence.

$$\sum_{n=1}^{\infty} \frac{5^n x^n}{1+2^n}$$

16. Also study the quizzes, and the homework questions. These are good test questions too!