## Presentation 2. Due by April 12. Outline due by March 26.

You must present on one of the following options.

1) Parts 7 and 8 of the linear program you considered for presentation 1.
a) Explain and use a greedy algorithm to solve your example problem.
b) Explain and use facet inequalities and an LP solver to solve your example problem.
2) Another linear programming problem no one has presented on yet: repeat of presentation 1. (parts 2-5 only)
3) A polytope sequence for which the entire face poset structure is known (see list below).
a) Describe the objects of the face poset. This means to define the combinatorial structures and their < relations-structures from column II below.
b) Give an example Hasse diagram for small dimension (2 or 3). Alternatively draw a small dimension polytope with all its faces labeled by objects from column II. (Or a 3d facet if the smallest available dimension larger than 2 is 4 .)
c) Show the polytope sequence for small dimensions (up to 3). You must label the vertices of the polytope with their actual vertex values and their associated object. (dim 4 for Birkhoff)
d) List some known facts about counting of faces.

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e) (Group work) Describe facet or face structures (self-similarity or skeleton lattice)

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f) (Groupwork) Describe another isomorphic poset structure, or a space tiling.
4) An algorithm for linear programming that we have not covered. (see list below).

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a) Describe the algorithm step by step.

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b) Give an example on a 2-dim LP that you make up (perform the alg on a polygon.

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c) (Groupwork) Give an example worked on a real-world problem (like STSP).

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Outline due by March 26: Give a brief, one sentence summary for the above chosen items. You may include terms that you don't understand completely yet. Make sure you list which parts will be presented by which partner if you plan to work as a team. Also give two dates on which you would like to do your presentation. (Tues Thurs, between April 12 and 19).

30 points total, worth $15 \%$ of grade.

Many polytopes and problems are summarized, with sources, here:
http://www.math.uakron.edu/~sf34/hedra.htm (The Associahedra Encyclopedia)

| I. Polytope | II. Poset (possibly alternate choices) |
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|  |  |
| Acyclotope (cycle graph) | Acyclic orientations of cycle graph |
| Birkhoff polytope | Perfect matchings of complete bipartite graph |
| Composihedron | Painted trees with corrollas |
| Cubeahedron(edgeless graph) | Design tubings of edgeless graph |
| Cyclohedron | Tubings of cycle graph |
| Diagonal rectangulation polytope | Miagonal Rectangulations |
| Graph composihedron (cycle graph) | Marked tubings of edgeless graph, with equivalence |
| Graph composihedron (edgeless graph) | Marked tubings of cycle graph |
| Graph multiplihedron (cycle graph) | Marked tubings of edgeless graph |
| Graph multiplihedron (edgeless graph) | Design tubings of cycle graph |
| Halohedron | Painted trees |
| Multiplihedron | Ordered partitions |
| Permutohedron/ permutahedron | Tubings of fan graph |
| LP Algorithm |  |
| Steepest-Edge simplex method |  |
| Devex Simplex method |  |
| Stellohedron |  |

